PHILIPPE BALBIANI, TINKO TINCHEV, Modal definability in Euclidean modal logics.

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A Kripke frame (W, R) is called Euclidean if the accessibility relation R satisfies the condition: for all $s, t, u \in W$, if sRt and tRu then tRu and uRt. A modal logic L is called Euclidean if it is determined by a nonempty class of Euclidean frames, i.e. if L is an extension of the modal logic K5. For every logic L, let Fr(L) be the class of all frames validating the theorems of L. A sentence A from the first-order language with equality and one binary predicate symbol is modally definable with respect to some class of frames if there is a modal formula φ from the classical propositional modal language such that A and φ are valid in the same frames from the class. Modal definability in a logic L problem asks whether there exists an algorithm that recognizes all modally definable with respect to Fr(L) sentences. Correspondence problem in a logic L asks whether there exists an algorithm that for any sentence A and any modal formula φ recognizes whether A and φ are valid in the same frames from Fr(L).

In this talk we present all Euclidean modal logics L such that the modal definability in L is decidable problem. We demonstrate also that these logics are exactly the Euclidean logics in which the correspondence problem is decidable.