

- BEIBUT KULPESHOV, *On algebras of binary formulas for weakly circularly minimal theories with a trivial definable closure.*

Institute of Mathematics and Mathematical Modeling, Kazakh-British Technical University, Almaty, Kazakhstan.

*E-mail:* b.kulpeshov@kbtu.kz.

Algebras of binary formulas are a tool for describing relationships between elements of the sets of realizations of 1-types at binary level with respect to superpositions of binary definable sets. We consider algebras of binary isolating formulas originally studied in [1, 2], where under a binary isolating formula we understand a formula of the form  $\varphi(x, y)$ , without parameters, such that for some parameter  $a$  the formula  $\varphi(a, y)$  isolates some complete type from  $S_1(\{a\})$ .

The notion of *weak circular minimality* was originally studied in [3]. A *weakly circularly minimal structure* is a circularly ordered structure  $M = \langle M, K_3, \dots \rangle$  such that any definable (with parameters) subset of  $M$  is a union of finitely many convex sets in  $M$ . In [4]  $\aleph_0$ -categorical 1-transitive non-primitive weakly circularly minimal structures of convexity rank 1 with a trivial definable closure have been described up to binarity.

Here we discuss algebras of binary isolating formulas for these structures and give the following criterion for commutability of such algebras:

**THEOREM 1.** *Let  $M$  be an  $\aleph_0$ -categorical 1-transitive non-primitive weakly circularly minimal structure of convexity rank 1 with  $\text{dcl}(a) = \{a\}$  for some  $a \in M$ . Then the algebra  $\mathfrak{P}_M$  of binary isolating formulas is commutable iff for any convex-to-right formula  $R(x, y)$  that is not equivalence-generating the function  $r(y) := \text{rend } R(M, y)$  is monotonic-to-right on  $M$ .*

This research has been funded by Science Committee of Ministry of Science and Higher Education of the Republic of Kazakhstan (Grant No. BR20281002).

[1] S.V. SUDOPLATOV, *Classification of countable models of complete theories*, Novosibirsk, Edition of NSTU, 2018.

[2] I.V. SHULEPOV, S.V. SUDOPLATOV, *Algebras of distributions for isolating formulas of a complete theory*, *Siberian Electronic Mathematical Reports*, Vol. 11 (2014), pp. 362–389.

[3] B.SH. KULPESHOV, H.D. MACPHERSON, *Minimality conditions on circularly ordered structures*, *Mathematical Logic Quarterly*, Vol. 51, No. 4 (2005), pp. 377–399.

[4] B.SH. KULPESHOV, *On  $\aleph_0$ -categorical weakly circularly minimal structures*, *Mathematical Logic Quarterly*, Vol. 52, No. 6 (2006), pp. 555–574.