

- CYRUS F NOURANI, PATRIK EKLUND, *Ultrafilters on n-types categories and the V Universe.*

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Let us start with n-types and positive local realizability (Keiser 1971, Nourani 2003): Given a theory  $T$  and a nonnegative integer  $n$ , let  $n(T)$  be the set of all signature  $(\phi) \subseteq \text{signature}(T)$ .

Let us consider (a) An ordinary category on T-Sigma trees for a signature Sigma and Sigma homomorphisms. (b) Category of direct product models realizing an n-Type: e.g. Horn filters (Nourani 2007). c. Term functors direct “product algebra” category. Objects are term functors and morphisms are natural transformations on representation presheaves (Nourani 2006). Call these nD-type embedding categories, or F-Type categories. Theorem 1 There is a generic functor on the category the omitting n-types realizing a direct product model (Nourani 2016). From Nourani 2015 volume: algebraic set theory:  $\forall$  onto the Boolean models,  $\forall\forall$ B, e.g. Scott models for classes of Boolean algebras can be reduced to only the Boolean algebras over  $\{0, 1\}$ . Proposition (Nourani 2005) stipulations on  $\forall\forall$  and be carried on  $\forall\forall$ B applying generic definable diagrams on set models, e.g. Gödel operations definable. From Kiesler 70’s: Theorem 2 Let  $T$  be a countable theory. For each  $i \in \omega$ , let  $\pi_i$  be an essentially nonprincipal n-type over  $T$ . Then  $T$  has a model which omits  $\pi_i$  for each  $i \in \omega$ . Let  $P(T \text{ Sig})$  be a functor category defined on the free signature trees with the power set on  $T \text{ Sig}$ , this can be a monoidal category. The adjunction functors being the functor  $F$ , forgetful to the product signature n-type category with  $G$  the embedding functor from the n-type category on the product pair signature to a powerset category. Lemma  $F.G$  is a Monad on pair product signature n-type. Theorem 3 There are embedding functors from F-Type to the direct product category realizing a filter for the product algebra trees on nD-types. (Nourani-Eklund 2016 MAA and, AAA Vienna2018)

[1] Nourani-Eklund 2017: Term Functors, Ultrafilter Categorical Computing, and Monads Cyrus F Nourani and Patrik Eklund: Coauthors. LAMBERT Academic Publishing Bahnhofstraße 28, D-66111 Saarbrücken, Germany).