

- BERNHARD STOINSKI, *Extension of category theory using a PL0 calculus functor to form propositional morphisms in multi-agent systems.*

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Abstract: The subject of this talk are morphisms between categories that are able to map truth values by means of a PL0-calculus functor  $Calc_0$ . This functor is used in the generation of AI multi-agent systems (MAS) [3]. In this case, the agents are equivalent to the categories [1]. A highly simplified example of an AI-MAS using PL0 calculus functors represents the practical aspect of this talk [2]. The special feature of the functor  $Calc_0 : A \rightarrow B$  is that the morphism from agent  $A$  to agent  $B$  yields a truth value  $t_A : X \rightarrow [0, 1]$ , taking  $A$  to be a fuzzy set. The function value  $m_A(a)$  for  $a \in X$  is itself again the membership value formed by the result of a calculus function of  $A$ . Hereby  $A$  itself becomes a fuzzy set. By this fact, a fuzzy space is formed by means of  $Calc_0$ , which, however, must not be confused with a type 2 fuzzy set. Through this construct and the self-similarity of the MAS, it is possible to represent complex natural processes with a high entropy [4] content.

[1] Mac Lane, S.. *Categories for the working Mathematician, Second Edition*, Springer Science+Business Media LLC, New York, 1971.

[2] RUST, S.; STOINSKI, B., *Using Artificial Intelligence to assist Tree Risk Assessment*, Using Artificial Intelligence to assist Tree Risk Assessment, Arboriculture and Urban Forestry, 48, No 2, P. 138-146, 2022.

[3] STOINSKI, B., *Dynamische Multi-Agent-Systeme Komplexe KI-Systeme: Wann ein kognitiver Ansatz wichtig ist.*, Industry-Of-Things, <https://www.industry-of-things.de/komplexe-ki-systeme-wann-ein-kognitiver-ansatz-wichtig-ist-a-06245d3c0db2a1902d95ac3a217f7630/>, 2022.

[4] SZILARD, L., *Über die Entropieverminderung in einem thermodynamischen System bei Eingriffen intelligenter Wesen*, , Zeitschrift für Physik 53, , 1929.